

On Pareto Set for a Bi-criterion Scheduling Problem Under Fuzziness

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Abstract

In this paper a bi-criterion fuzzy scheduling problem was presented and the problem under consideration is total fuzzy completion time and maximum earliness, where the processing times and the due dates are triangular fuzzy numbers. Each of n jobs is to be processed without interruption on a single machine and becomes available for processing at time zero. A new definition of fuzzy numbers was given namely m -strongly positive fuzzy numbers, through this definition we found an interval which restricts the range of the fuzzy lower bound and presented a relation between the fuzzy lower bound and the fuzzy optimal solution with number of efficient solutions. Also we found the exact solution of the problem through finding the Pareto set.

Keywords: Scheduling problem, Bi-criterion problems, Pareto set, Fuzzy processing times, Fuzzy due dates.

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1. Introduction

Different approaches to fuzzy multi-objective have been considered with fuzzy parameters (Duenas and Petrovic, 2008). (Ishii and Tada, 1995) studied the maximum tardiness with fuzzy precedence relation. An extensive review of scheduling problems with multi-objectives was introduced by (T'kindt and Billaut, 2001) where they focused on single machine scheduling, parallel-machine scheduling, flow shop and fuzzy scheduling problems.

Many research articles in scheduling problems dealt with earliness penalties. (Jayanthi et al., 2017) minimized earliness and tardiness costs where both processing times and due dates are fuzzy (Niroomand et al., 2016) focused on a problem of minimizing earliness and tardiness with common fuzzy due date on a single machine.

Two important types of bi-criteria scheduling problems are there, the hierarchical problems and the simultaneous problems. Simultaneous problems mean that the two objectives have the same importance. In this case a Pareto set can be found which provides deeper insights to the decision maker to choose one of these solution (Lei, 2009). Many important works were done regarding Pareto set. (Hoogeveen and Velde, 1995) minimized total completion time and maximum cost simultaneously. For equal processing times with respect to criteria L_{max} and C_{max} (Lazarev et al., 2015) found the Pareto set for these jobs. (Nguyen and Bao, 2016) found the efficient solution to the mixed shop scheduling problem by using genetic algorithm. (Abdul-Razaq and Kawi, 2010) solved simultaneously a function of square completion time and maximum tardiness.

In this paper a bi-criterion scheduling problem is studied which is minimize total fuzzy

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completion time and maximum fuzzy earliness. A new definition of fuzzy numbers is introduced, a relation between the lower bound and the optimal solution with number of efficient solutions for a problem is given. Also an exact solution of the problem was found through the Pareto set.

2. Definitions and Notations

Definition 1. Triangular fuzzy number is a fuzzy number represented by three points $\tilde{A} = (a^L, a, a^U)$. The membership function of a triangular fuzzy number \tilde{A} is defined by

$$\mu_{\tilde{A}}(x) = \begin{cases} 0 & , x < a^L, \\ \frac{x-a^L}{a-a^L} & , a^L \leq x \leq a, \\ \frac{a^U-x}{a^U-a} & , a < x \leq a^U. \end{cases}$$

Suppose that \tilde{A} and \tilde{B} are two triangular fuzzy numbers where $\tilde{A} = (a^L, a, a^U)$ and $\tilde{B} = (b^L, b, b^U)$, then

- (i) $\tilde{A} \oplus \tilde{B} = (a^L + b^L, a + b, a^U + b^U)$, which is also triangular fuzzy number,
- (ii) $\tilde{A} \ominus \tilde{B} = (a^L - b^U, a - b, a^U - b^L)$, which is also triangular fuzzy number (Hsien, 2010).

To find a crisp value of the triangular fuzzy number, the procedure that converts a fuzzy number to its crisp value is called defuzzification. Consider the following triangular fuzzy number $\tilde{A} = (a_1, a_2, a_3)$ the centroid point method of the triangular fuzzy number is $D(\tilde{A}) = \frac{a_1 + a_2 + a_3}{3}$ (Cheng, 1998). Let \tilde{p}_1 and \tilde{p}_2 be two triangular fuzzy processing times where $\tilde{p}_1 = (p_1^L, p_1, p_1^U)$ and $\tilde{p}_2 = (p_2^L, p_2, p_2^U)$, also for the due dates \tilde{d}_1 and \tilde{d}_2 be two triangular fuzzy due dates where $\tilde{d}_1 = (d_1^L, d_1, d_1^U)$ and $\tilde{d}_2 = (d_2^L, d_2, d_2^U)$. Most of the defuzzification methods lead to a rational numbers, so let F be the denominator of the rational number which has a great role in this paper.

N: the set $\{1, 2, 3, \dots, n\}$,

Π : the set of permutation schedules,

$\tilde{p}_j = (p_j^L, p_j, p_j^U)$: fuzzy processing time of job j, and they are triangular fuzzy numbers (TFN),

$\tilde{d}_j = (d_j^L, d_j, d_j^U)$: fuzzy due date of job j,

\tilde{c}_j : fuzzy completion time of job j,

$\tilde{E}_j = \tilde{m}\tilde{a}\tilde{x} \{ \tilde{d}_j \ominus \tilde{c}_j, \tilde{0} \}$: fuzzy earliness of job j, where $\tilde{0} = (0, 0, 0)$,

$\tilde{E}_{\max} = \tilde{m}\tilde{a}\tilde{x} \{ \tilde{E}_j \}$: maximum fuzzy earliness,

A^c : crisp value of the fuzzy number \tilde{A} ,

F: the denominator of a rational number, and can be teated as a fuzzy number as $\tilde{F}_j = (F_j, F_j, F_j)$,

i.e. $F_j^L = F_j = F_j^U$,

MST (Minimum fuzzy slack times): jobs are sequenced in non-decreasing order of minimum fuzzy slack times \tilde{s}_j , where $\tilde{s}_j = \tilde{d}_j \ominus \tilde{p}_j$,

SPT (Shortest processing time): jobs are sequenced in non-decreasing order of \tilde{p}_j ,

$\tilde{L}\tilde{B}$ (Fuzzy lower bound): is a value of the objective function which is less than or equal to the fuzzy optimal value,

$\tilde{U}\tilde{B}$ (Fuzzy upper bound): is a value of the objective function which is greater than or equal to the

fuzzy optimal value.

Definition 2. A feasible schedule $\pi^* \in \Pi$ is Pareto optimal, or efficient, with respect to the criteria f_1 and f_2 if there is no feasible schedule π such that both $f_1(\pi) \leq f_1(\pi^*)$ and $f_2(\pi) \leq f_2(\pi^*)$, where at least one of the inequalities is strict.

3. Structure of the Problem

It is important to introduce some structures of bi-criteria problems to understand the relation among their solutions as illustrated in the following table.

Let f_1 and f_2 be two criteria, then

Types	Structures	Notes	Possible solutions
I	f_1 s.t. f_2	Hierarchical problems 1//Lex(f_2, f_1)	Optimal solution
II	f_1 and f_2	Simultaneous problems 1//F(f_1, f_2)	Pareto set, no optimal solution
III	f_1+f_2	Sum of two problems	Optimal solution

Now consider a set $N, N = \{1, 2, \dots, n\}$ of n jobs to be processed on a single machine without interruption. Each job j has a triangular fuzzy processing time $\tilde{p}_j = (p_j^L, p_j, p_j^U)$, and a triangular fuzzy due date $\tilde{d}_j = (d_j^L, d_j, d_j^U)$, for $j = 1, 2, \dots, n$. All jobs are available at time zero and the machine can only process one job at a time. The objective functions under study are $f_1 = \sum_{j=1}^n \tilde{c}_j$ and $f_2 = \tilde{E}_{max}$.

For the problem (III), let the fuzzy lower bound $\tilde{LB} = \sum_{j=1}^N \tilde{c}_j(SPT) \oplus \tilde{E}_{max}(MST)$ and the fuzzy upper bound $\tilde{UB} = \sum_{j=1}^N \tilde{c}_j(SPT) \oplus \tilde{E}_{max}(SPT)$, where the fuzzy completion time of jobs can be calculated according to the following formulas:

$$\begin{aligned} \tilde{c}_1 &= \tilde{p}_1, \\ \tilde{c}_2 &= \tilde{c}_1 \oplus \tilde{p}_2, \\ &\vdots \\ \tilde{c}_j &= \tilde{c}_{j-1} \oplus \tilde{p}_j, \text{ for } j = 1, \dots, n. \end{aligned} \quad (1)$$

The fuzzy earliness is defined as a fuzzy maximum of zero and the difference between the fuzzy due date and the fuzzy completion time of this job, this means

$$\tilde{E}_j = \overline{\max} \{ \tilde{d}_j \ominus \tilde{c}_j, \tilde{0} \}, \quad (2)$$

where the fuzzy completion time $\tilde{c}_j = (c_j^L, c_j, c_j^U)$ of each job j and can be obtained by Eq.(1) and maximum fuzzy earliness is

$$\tilde{E}_{max} = \overline{\max} \{ \overline{\max} \{ \tilde{d}_j \ominus \tilde{c}_j, \tilde{0} \} \} [11].$$

(3)

4. Pareto Set in Fuzzy Environment

It is known that the minimum slack time MST-rule, if no idle time is allowed, E_{max} is minimized by sequencing the jobs in of non-decreasing order of $s_j = d_j - p_j$. Since E_{max} is irregular function then the value of E_{max} is in the range $[E_{max}(MST), E_{max}(SPT)]$. (Hoogeveen and Velde, 1995) minimized total completion time and maximum cost simultaneously in polynomial time. (Kurz and Canterbury, 2005) found the Pareto set for the same problem by using genetic algorithm.

In the fuzzy environment the problem (II) is $1//F(\sum_{j=1}^N \tilde{c}_j, \tilde{E}_{max})$. We will present a new definition of fuzzy numbers, and then introduce our results.

4.1. M-strongly positive numbers

Definition 3. Two fuzzy numbers $\tilde{A} = \{a^L, a, a^U\}$ and $\tilde{B} = \{b^L, b, b^U\}$ are said to be m-strongly positive iff $(a^L + a + a^U) - (b^L + b + b^U) \geq m$, where m is any positive number greater than or equal 1.

Theorem 1. If the fuzzy processing times are comparable with the ordering " \leq " by one of the ranking methods, then the SPT sequence is one of the efficient solutions.

Proof. Suppose that all $p_j^c, j = 1, 2, \dots, n$ are different, so the unique SPT sequence gives the absolute minimum of f_1 . Hence there is no sequence π such that $f_1(\pi) \leq f_1(SPT)$. If more than one SPT sequence exists, let SPT^* be a sequence satisfying the SPT-rule and such that jobs with equal p_j^c are in MST sequence. Hence there is no sequence π such that $f_1(\pi) < f_1(SPT^*)$. So the SPT is one of the efficient solution. \square

In general the MST sequence must not be an efficient solution, it is possible to a sequence to have the same value as the MST sequence has.

Let $\tilde{p}_j = (p_j^L, p_j, p_j^U)$, $1 \leq j \leq n$ be a fuzzy processing time, and p_j^c be its corresponding crisp value. According to the above defuzzify method $D(\tilde{p}_j) = p_j^c = \frac{p_j^{c*}}{3} = \frac{p_j^L + p_j + p_j^U}{3}$. Also for $D(\tilde{d}_j) = d_j^c = \frac{d_j^{c*}}{3} = \frac{d_j^L + d_j + d_j^U}{3}$. For the fuzzy earliness $\tilde{E}_j = \{E_j^L, E_j, E_j^U\}$, $1 \leq j \leq n$, E_j^c is the crisp value and can be found in the same way.

5. An algorithm

We introduce an algorithm which finds all efficient solutions (Pareto set) for the problem (II).

Step (0): Compute $\tilde{E}_{max}(MST)$, and $\tilde{E}_{max}(SPT)$, let $k = 1$, $\tilde{E}_{max}(SPT) = E^*$.

Step (1): Solve $1//Lex(\tilde{E}_{max}, \sum_{j=1}^n \tilde{c}_j)$ [10].

Step (2): $E^* = E^* \ominus F$, $k = k + 1$.

Step (3): If $E^* < \tilde{E}_{max}(\text{MST})$ stop, else, go to step (1).

Theorem 2. The algorithm generates all the efficient solutions of the problem (II) if the efficient solutions are m -strongly positive fuzzy numbers and $m \geq F$.

Proof. Since the efficient solutions $(\alpha_1, \alpha_2, \dots, \alpha_k)$, where $k < n!$ are m -strongly positive, so the difference between $E_{max}^c(\alpha_i)$ and $E_{max}^c(\alpha_{i+1})$ is $\geq m$, $1 \leq i \leq k - 1$.

Let

$$E_{max}^c(\alpha_i) = \frac{E_{max}^{c*}(\alpha_i)}{F} \quad \text{and} \quad E_{max}^c(\alpha_{i+1}) = \frac{E_{max}^{c*}(\alpha_{i+1})}{F} \quad 1 \leq i \leq k - 1.$$

Therefore, the difference between $\frac{E_{max}^{c*}(\alpha_i)}{F}$ and $\frac{E_{max}^{c*}(\alpha_{i+1})}{F}$ is $\frac{m}{F}$, $1 \leq i \leq k - 1$. In the steps of the algorithm we find a sequence of fuzzy earliness \tilde{E}_{max} , and the difference between each one is m -strongly positive. To apply the step (2) of the algorithm, we have

$$\frac{E_{max}^{c*}(\alpha_i)}{F} - F,$$

so if $m < F$ then the next solution may lead to an infeasible solution(not efficient solution). Therefore m must be greater than or equal to F .

□

Consider the set of maximum fuzzy earliness $S = \{\tilde{E}_{max}(\sigma_i)\}$ and the set of total fuzzy completion time $S_1 = \{\sum_{j=1}^N \tilde{c}_j(\sigma_i)\}$, where each two elements in both sets are m -strongly positive, this means that $\tilde{E}_{max}(\sigma_i)$ and $\tilde{E}_{max}(\sigma_{i+1})$ are m -strongly positive, and $\sum_{j=1}^N \tilde{c}_j(\sigma_{i+1})$ and $\sum_{j=1}^N \tilde{c}_j(\sigma_i)$ are m -strongly positive too, $\forall i, i = 1, \dots, k$. k is number of efficient solutions. Let \tilde{opt} be the fuzzy optimal value of the problem (III).

Theorem 3. If the efficient solutions are 3-strongly positive numbers of the problem (II), then there exists a fuzzy number \tilde{r} such that $\tilde{LB} \oplus \tilde{r} = \tilde{opt}$ and $r^c \in [N_1 - 1, (\tilde{N}_2 \oplus \frac{1}{F})^c]$ where $N_1 =$ number of efficient solutions and $\tilde{N}_2 = \tilde{E}_{max}(\text{SPT}) \ominus \tilde{E}_{max}(\text{MST})$.

Proof. Since $\tilde{LB} \leq \tilde{opt}$, so there exists \tilde{r} such that $\tilde{LB} \oplus \tilde{r} = \tilde{opt}$ which proves the first part of the theorem. It remains to show that $r^c \in [N_1 - 1, (\tilde{N}_2 \oplus \frac{1}{F})^c]$ or to show that $N_1 - 1 \leq r^c \leq (\tilde{N}_2 \oplus \frac{1}{F})^c$. We have $\tilde{r} = \tilde{opt} \ominus \tilde{LB} \leq \tilde{UB} \ominus \tilde{LB}$

$$= \tilde{E}_{max}(\text{SPT}) \ominus \tilde{E}_{max}(\text{MST})$$

$$= \tilde{N}_2 \leq \tilde{N}_2 \oplus \frac{1}{F},$$

implies that $r^c \leq (\tilde{N}_2 \oplus \frac{1}{F})^c$.

To prove $N_1 - 1 \leq r^c$ we will use the mathematical induction on N_1 .

If $N_1 = 1$, that is, there is only one efficient solution which is *SPT* then

$$\tilde{r} = \sum_{j=1}^N \tilde{c}_j(\text{SPT}) \oplus \tilde{E}_{max}(\text{SPT}) \ominus \sum_{j=1}^N \tilde{c}_j(\text{SPT}) \ominus \tilde{E}_{max}(\text{MST}),$$

$$= \tilde{E}_{max}(SPT) \ominus \tilde{E}_{max}(MST),$$

since $\tilde{E}_{max}(SPT)$ and $\tilde{E}_{max}(MST)$ are equal , so

$$r^c = 0.$$

Thus $r^c = 0 = N_1 - 1$, so the theorem is true for $N_1 = 1$.

If $N_1 = 2$, that is, the number of efficient solutions is two which are SPT and σ , say. Since $N_1 = 2$, so $N_1 - 1 = 1$. We have the following two cases:

a- If SPT is fuzzy optimal then

$$\begin{aligned} \tilde{r} &= \sum_{j=1}^N \tilde{c}_j(SPT) \oplus \tilde{E}_{max}(SPT) \ominus \sum_{j=1}^N \tilde{c}_j(SPT) \ominus \tilde{E}_{max}(MST), \\ &= \tilde{E}_{max}(SPT) \ominus \tilde{E}_{max}(MST), \end{aligned}$$

since $\tilde{E}_{max}(SPT)$ and $\tilde{E}_{max}(MST)$ are strongly positive , so

$$E_{max}^c(SPT) - E_{max}^c(MST) \geq 1.$$

Thus $r^c \geq 1 \geq N_1 - 1$, so the theorem is true for $N_1 = 2$.

b- If σ is fuzzy optimal then

$$\begin{aligned} \tilde{r} &= \sum_{j=1}^N \tilde{c}_j(\sigma) \oplus \tilde{E}_{max}(\sigma) \ominus \sum_{j=1}^N \tilde{c}_j(SPT) \ominus \tilde{E}_{max}(MST), \\ &= \sum_{j=1}^N \tilde{c}_j(\sigma) \ominus \sum_{j=1}^N \tilde{c}_j(SPT), \end{aligned}$$

since they are strongly positive , so

$$r^c \geq 2 \geq N_1 - 1,$$

so the theorem is true for $N_1 = 2$.

If $N_1 = 3$, that is, the number of efficient solutions is three which are SPT, σ and σ_1 , say. Since $N_1 = 3$, so $N_1 - 1 = 2$. We have the following three cases:

(a) If SPT is fuzzy optimal then

$$\begin{aligned} \tilde{r} &= \sum_{j=1}^N \tilde{c}_j(SPT) \oplus \tilde{E}_{max}(SPT) \ominus \sum_{j=1}^N \tilde{c}_j(SPT) \ominus \tilde{E}_{max}(MST), \\ &= \tilde{E}_{max}(SPT) \ominus \tilde{E}_{max}(MST), \end{aligned}$$

since $\tilde{E}_{max}(SPT)$ and $\tilde{E}_{max}(MST)$ are strongly positive , so

$$E_{max}^c(SPT) - E_{max}^c(MST) \geq 2.$$

Thus $r^c \geq 2 \geq N_1 - 1$, so the theorem is true for $N_1 = 3$.

(b) If σ is fuzzy optimal then

$$\begin{aligned} \tilde{r} &= \sum_{j=1}^N \tilde{c}_j(\sigma) \oplus \tilde{E}_{max}(\sigma) \ominus \sum_{j=1}^N \tilde{c}_j(SPT) \ominus \tilde{E}_{max}(MST), \\ &= \sum_{j=1}^N \tilde{c}_j(\sigma) \ominus \sum_{j=1}^N \tilde{c}_j(SPT) \oplus \tilde{E}_{max}(\sigma) \ominus \tilde{E}_{max}(MST), \end{aligned}$$

since each of the difference is strongly positive , so

$$r^c \geq 2 \geq N_1 - 1,$$

so the theorem is true for $N_1 = 3$.

(c) If σ_1 is fuzzy optimal then

$$\tilde{r} = \sum_{j=1}^N \tilde{c}_j(\sigma_1) \oplus \tilde{E}_{max}(\sigma_1) \ominus \sum_{j=1}^N \tilde{c}_j(SPT) \ominus \tilde{E}_{max}(MST),$$

$$\begin{aligned}
&= \sum_{j=1}^N \tilde{c}_j(\sigma_1) \ominus \sum_{j=1}^N \tilde{c}_j(\text{SPT}) \oplus \tilde{E}_{\max}(\sigma_1) \ominus \tilde{E}_{\max}(\text{MST}), \\
&= \sum_{j=1}^N \tilde{c}_j(\sigma_1) \ominus \sum_{j=1}^N \tilde{c}_j(\text{SPT})
\end{aligned}$$

since they are strongly positive , so

$$r^c \geq 2 \geq N_1 - 1,$$

so the theorem is true for $N_1 = 3$.

Suppose the theorem is true for $N_1 = k$, that is, the theorem is true for the k efficient solutions SPT, $\sigma, \sigma_1, \dots, \sigma_{k-2}$. Let $N_1 = k + 1$, that means, there are $k + 1$ efficient solutions SPT, $\sigma, \sigma_1, \dots, \sigma_{k-2}, \sigma_{k-1}$. If any one of the first k efficient solutions is fuzzy optimal and as the theorem is true for $N_1 = k$ we get $N_1 - 1 \leq r^c$.

If the last efficient solution σ_{k-1} is fuzzy optimal then

$$\tilde{r} = \sum_{j=1}^N \tilde{c}_j(\sigma_{k-1}) \oplus \tilde{E}_{\max}(\sigma_{k-1}) \ominus \sum_{j=1}^N \tilde{c}_j(\text{SPT}) \ominus \tilde{E}_{\max}(\text{MST}),$$

implies that

$$\tilde{r} = \sum_{j=1}^N \tilde{c}_j(\sigma_{k-1}) \ominus \sum_{j=1}^N \tilde{c}_j(\text{SPT}),$$

and then $r^c \geq k$. Thus the theorem is true for $N_1 = k + 1$. \square

6. Conclusion and Discussion

In this paper, we investigated the problem which was the total fuzzy completion time and maximum earliness, where the processing times and the due dates are triangular fuzzy numbers. We presented a new structure of fuzzy number, and through this we found a relation between the fuzzy lower bound and the fuzzy optimal solution with number of efficient solutions. This relation restricted the range of the fuzzy lower bound which is a main factor to find an optimal solution. Also we found the exact solution under this structure, through finding the Pareto set.

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