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## Using Three Statistical Analyses for Studying the Total Water Hardness of Tigris River in Mosul Town

### Abstract

Three statistical analyses were applied: analysis of variance and then the multistatistical comparisons represented by the test of Newman-Keul, the quality control procedure and the cluster analysis, to compare between the results of their analyses on the data represented a chemical specification by water hardness (ml/l) of Tigris river in Mosul town. The samples were taken from five sites which are: Darnajook, Shouhada'a bridge, Nineveh bridge, Danadan and Yaremjah.

Some matched results were noticed between Newman-Keul test and the quality control procedure, while cluster analysis gave different results.

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[67] .....

(70%)

.(2006, )

.(2008 , )

Kanber (1973)

(1983)

(1999)

( )

(2005)

(2008)

(2011)

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( / )

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:(One way analysis of variance)

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(Response)

(Between groups variation)

:

(Within variation)

هي قيمة الاستجابة  $y_{ij}$  وأن  $(i = 1, \dots, k)$   $n_i$   $k$

التي تعكسها المشاهدة  $j$  ( $j = 1, \dots, n$ ) في المجموعة  $i$  (Montgomery: 2009).

( )

$(\mu_1, \dots, \mu_k)$

:

$(\sigma_1^2 = \dots = \sigma_k^2 = \sigma_\epsilon^2)$

$H_0: \mu_1 = \dots = \mu_k$

$H_1: \text{At least one mean is differ.}$

(1)

$(H_0)$

(Multiple

comparisons)

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S.O.V	d.f	Sum Of Squar	Meam Of Squar	F
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بين المجموعات Between groups	$k - 1$	$SSG$	$MSG = \frac{SSG}{k-1}$	$\frac{MS_{BG}}{MS_{WG}}$
الخطأ Within groups	$k(n - 1)$	$SSE$	$MSE = \frac{SSE}{k(n-1)}$	
Total	$nk - 1$	$SST$		

(Newman-Keul's test)

( $\alpha$ )

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(2010 )

**:Quality control -2**

(Control)

(Quality)

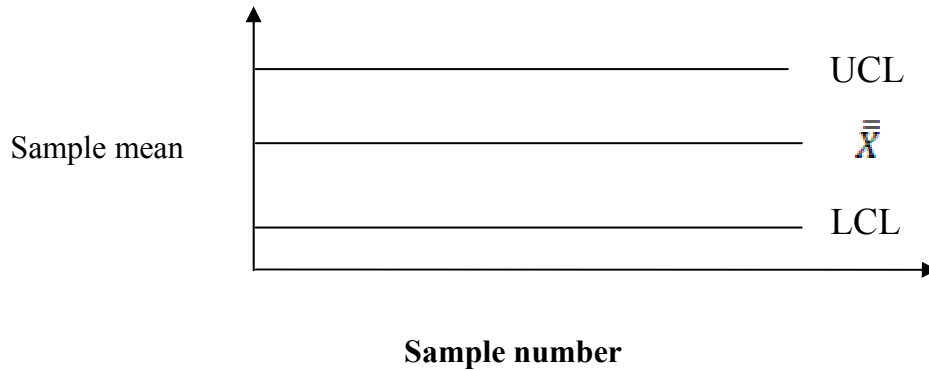
(2007 )

(Statistical quality control)

(Variables control charts)

(Average chart) ( $\bar{X}$ - )

المعدل  
(1) (  $\bar{\bar{X}}$  ) (2007).



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$$\text{Centerline (T)} = \bar{\bar{X}} = \frac{\sum_{j=1}^k \bar{X}_j}{k} \dots\dots (1)$$

$$\text{Upper control limit (UCL)} = \bar{\bar{X}} + c\sigma_{\bar{x}} \dots\dots (2)$$

$$\text{Lower control limit (UCL)} = \bar{\bar{X}} - c\sigma_{\bar{x}} \dots\dots (3)$$

$$\sigma_{\bar{x}} = \frac{\sigma_x}{\sqrt{N}} \dots\dots (4)$$

$$\sigma_x = \sqrt{\frac{\sum_{i=1}^k \sum_{j=1}^n (x_{ij} - \bar{X}_i)^2}{nk}} \dots\dots (5)$$

3 2 1 =c =n =k

(2011) LCL UCL

:(Cluster analysis)

.(Xu & Wunsch, 2009)

(D)

$$\underline{D} = \begin{bmatrix} 0 & d_{12} & \dots & d_{1m} \\ d_{21} & 0 & \dots & d_{2m} \\ \dots & \dots & 0 & \dots \\ \dots & \dots & \dots & \dots \\ d_{m1} & d_{m2} & \dots & 0 \end{bmatrix}$$

:  $i'$   $i$   $(d_{ii'})$

$$d_{ii'} = \sqrt{\sum_{j=1}^n (x_{ij} - x_{i'j})^2} \dots \dots \dots (6)$$

Similarity coefficient ( $S_{ii'}$ )

$$S_{ii'} = \frac{100(1-d_{ii'})}{d(max)} \dots \dots \dots (7)$$

:  $d(max)$

:(Hierarchical tree diagram)

Dendrogram

(Rao &

.Srinivas, 2008)

(Weighted centroid method)

$$w. c. linkage (i, i') = \frac{n_i d_{ik} + n_{i'} d_{i'k}}{n_i + n_{i'}} - \frac{n_i n_{i'} d_{ii'}}{(n_i + n_{i'})^2} \dots \dots \dots (8)$$



$$\begin{matrix} i' & i \\ i' & i \end{matrix} = n_{i'}, n_i = k$$

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(2001)

( / )  
 (X<sub>5</sub>) (X<sub>4</sub>) (X<sub>3</sub>) (X<sub>2</sub>) (X<sub>1</sub>)  
 150 2000000  
 (2 )  
 (2011 ) (3)

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56.76	278.86	
54.12	288.48	
56.01	289.61	
50.41	299.66	
49.07	296.35	

( / )

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( / )	
0 - 75	
75 - 150	
150 - 300	
300 - 500	
500	

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( $\alpha$ )

( $\alpha$ )

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$H_0: \mu_1 = \dots = \mu_5$ .

$H_1: \text{At least two means are not equal.}$

.(4)

SPSS v. 11.5

:4

S.O.V	S.S.	d.f.	M.S.	F	P. value
Between groups	38755.019	4	9688.755	3.402	0.009
Within groups	2121473	745	2847.615		
Total	2160228	749			

(4)

$\alpha > 0.853$

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$\alpha = 0.853$

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. $\alpha = 0.853$

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Variable		Subset for alpha=0.853
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	N	1	2	3	4
X <sub>1</sub>	150				
X <sub>2</sub>	150		288.477		
X <sub>3</sub>	150		289.672		
X <sub>5</sub>	150			296.345	
X <sub>4</sub>	150				299.655

( )  $\alpha = 0.591$   $\alpha$   
 .(6 ) ( )

. $\alpha = 0.591$  - :6

Variable	N	Subset for alpha=0.591		
		1	2	3
X <sub>1</sub>	150	278.857		
X <sub>2</sub>	150		288.477	
X <sub>3</sub>	150		289.672	
X <sub>5</sub>	150			296.345
X <sub>4</sub>	150			299.655

X<sub>3</sub> X<sub>2</sub>  $\alpha = 0.267$   
 . $\alpha = 0.007$  (7 ) X<sub>5</sub> X<sub>4</sub>

. $\alpha = 0.267$  :7

Variable	N	Subset for alpha=0.267	
		1	2
X <sub>1</sub>	150	278.857	
X <sub>2</sub>	150		288.477
X <sub>3</sub>	150		289.672
X <sub>5</sub>	150		296.345
X <sub>4</sub>	150		299.655

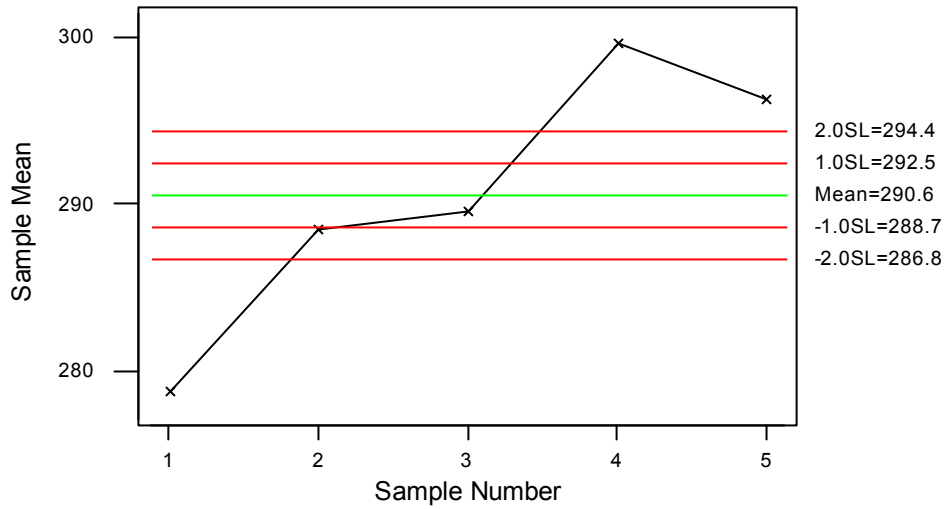
( ) (7)

$\alpha \leq 0.006$

[75]

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(1 ) (290.590) (2 )  
. (4 ) (1.900)



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.(2008 )

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(Agglomerative method)

(7 )

(6 )

(10)

(8 )

Cluster observation

:10

<b>2</b>	<b>y<sub>1</sub></b>	<b>X<sub>3</sub></b>	<b>X<sub>1</sub></b>	<b>197.442</b>	<b>37.300</b>	<b>4</b>	<b>1</b>
<b>3</b>	<b>y<sub>2</sub></b>	<b>X<sub>2</sub></b>	<b>y<sub>1</sub></b>	<b>176.818</b>	<b>43.850</b>	<b>3</b>	<b>2</b>
<b>4</b>	<b>y<sub>3</sub></b>	<b>X<sub>4</sub></b>	<b>y<sub>2</sub></b>	<b>204.643</b>	<b>35.020</b>	<b>2</b>	<b>3</b>
<b>5</b>	<b>y<sub>4</sub></b>	<b>X<sub>5</sub></b>	<b>y<sub>3</sub></b>	<b>189.004</b>	<b>39.980</b>	<b>1</b>	<b>4</b>

: (10)

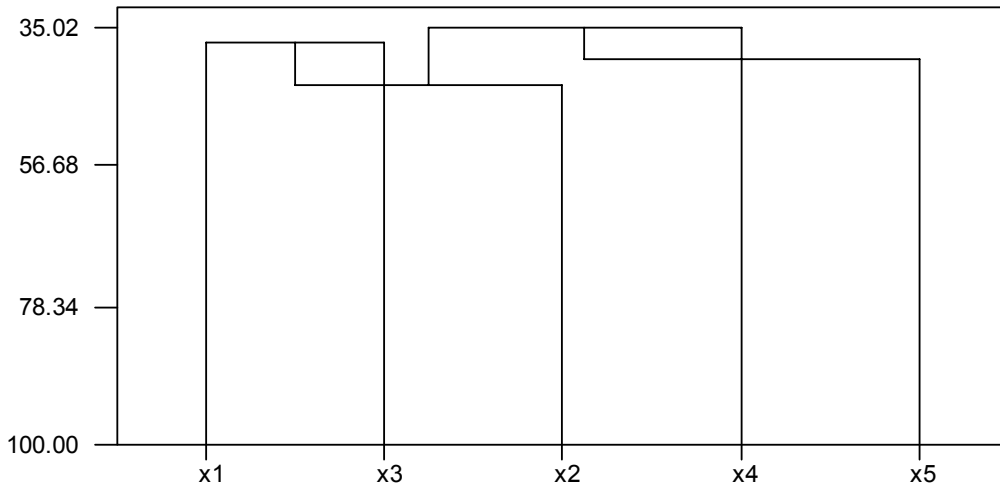
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) (Dendrogram)

(3)



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:(3 ) (10 ) (2 ) (7 6

(5 )  $\alpha = 0.853$  - : -1

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(2 )

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(6 )  $\alpha = 0.591$  - : -2

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$\alpha = 0.267$  - : -3

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(11)

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$X_3 \quad X_2$			
$X_4$			
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